

U-3725

B.C. A. (Sixth Semester)

EXAMINATION, May/June, 2018

Paper-I

PROBABILITY AND STATISTICS

Time : Three Hours

Maximum Marks : 80 (For Regular Students)

Minimum Pass Marks : 32

Note-Attempt all questions. Solve any two parts from each question. All questions carry equal marks.

Unit - I

1. (a) Write short notes on the following-

(i) Histogram (ii) Cumulative frequency distribution.

(b) Find Mean of the following data-

Age (in years) No. of students

| | |
|----------------|-----------|
| 10 - 19 | 1 |
| 20 – 29 | 0 |
| 30 - 39 | 1 |
| 40 - 49 | 10 |
| 50 - 59 | 17 |
| 60 - 69 | 38 |
| 70 - 79 | 9 |
| 80 - 89 | 3 |

(c) Calculate the coefficient of variation of the following distribution:

| | |
|------------|------------------|
| x | Frequency |
| 102 | 3 |
| 106 | 9 |
| 110 | 25 |

| | |
|-----|----|
| 114 | 35 |
| 118 | 17 |
| 122 | 10 |
| 126 | 01 |

Unit - II

2. (a) Compute the first three moments about mean from the following data

| Class interval | Frequency |
|----------------|-----------|
| 0 - 10 | 1 |
| 10 - 20 | 3 |
| 20 - 30 | 4 |
| 30 - 40 | 2 |

(b) Find the moment generating function of the random variable 'X' having p.d.f.

$$f(x) = \begin{cases} x, & 0 \leq x < 1 \\ 2 - x, & 1 \leq x < 2 \\ 0, & \text{Otherwise} \end{cases}$$

(c) Three horses A, B and C are in a race. A is twice as likely to win as B and B is twice as likely to win as C. What are the respective probabilities of winning?

Unit - III

3. (a) Find the value of λ a for which the function is p.d.f. if

$$f(x) = \begin{cases} \lambda x^2, & 0 \leq x \leq 3 \\ 0, & \text{otherwise} \end{cases}$$

Also compute $P(1 \leq x \leq z)$.

(b) In a Poisson distribution, prove that mean and variance are same.

(c) Explain normal distribution and its properties.

Unit - IV

4. (a) Calculate the Karl Pearson's correlation coefficient between x and y:

| | |
|-----|----|
| x | y |
| 150 | 65 |

| | |
|------------|-----------|
| 153 | 66 |
| 154 | 67 |
| 155 | 70 |
| 157 | 68 |
| 160 | 53 |
| 163 | 70 |
| 164 | 63 |

(b) If $4x - 5y + 33 = 0$ and $20x - 9y = 107$ are two lines of regression. Find

(i) Mean value of x and y

(ii) Regression coefficients

(iii) Correlation coefficients.

(c) Fit a parabolic curve of regression of y on x to the following data

| x | y |
|-----|-----|
| 1.0 | 1.1 |
| 1.5 | 1.3 |
| 2.0 | 1.6 |
| 2.5 | 2.0 |
| 3.0 | 2.7 |
| 3.5 | 3.4 |
| 4.0 | 4.1 |

Unit- V

5. (a) Write short notes on the following-

(i) Null and alternative hypothesis.

(ii) Errors of Kind I and Kind II.

(b) From the table given below, whether the colour of son's eyes is associated with that of father's eyes ? Given that the value of chi-square for 1 d.f at 5% level of significance is 3.841.

Eye colour son's

| | | | |
|-------------------------|-----------|-----------|-------|
| Eye colour of father | | Not light | Light |
| | Not light | 230 | 148 |
| | Light | 151 | 471 |

(c) In a test given two groups of students drawn two normal populations, the marks obtained were as follows

| Group B | Group A |
|---------|---------|
| 18 | 29 |
| 20 | 28 |
| 36 | 26 |
| 50 | 35 |
| 49 | 30 |
| 36 | 44 |
| 34 | 46 |
| 49 | |
| 41 | |

Examine at 5% level of significance, whether the two populations have the same variance. (Given that

$$F_{0.05, (8,6)} = 4.15)$$